

QUESTION BANK

CLASS: FYBSC MATHS I TITLE :CALCULUS II

- Q 1 The value of 1
(a) $1/3$
(b) 1
(c) $3/4$
(d) 0

Ans : $3/4$

- 2 The value of 1
(a) 6
(b) 3
(c) 4
(d) 0

Ans : 6

- 3 If $f(x) = (\tan x)/x$, for $x \neq 0$ then $\lim_{x \rightarrow 0} f(x)$ 1
(a) 1
(b) 0
(c) 0
(d) -1

Ans (a)

- 4 Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined as $f(x) = \begin{cases} x, & \text{if } x < 0 \\ e^x, & \text{if } x \geq 0 \end{cases}$ then $\lim_{x \rightarrow 0^+} f(x)$ is

- (a) 0
(b) 1
(c) e
(d) Does not exist

Ans (b) -1

- 5 The value of $\lim_{x \rightarrow 0}$ 2
(a) -1
(b) 1
(c) 0
(d) Does not exist

Ans : (d)

- 6 If $f(x) = \begin{cases} 2x + 1 & \text{for } x < 0 \\ x - 1 & \text{for } x \geq 0 \end{cases}$ then $x = 0$ is a point at which the function f is 1

- (a) Continuous
 (b) Discontinuous
 (c) Decreasing
 (d) Does not exist
- 7 $F(x) = x^4 + x^2, x \in \mathbb{R}$ is 1
 (a) Continuous
 (b) Continuous only if $x > 0$
 (c) Discontinuous
 (d) Always negative
 Ans: (a)
- 8 The value of $\lim_{x \rightarrow 0} (x^2 - 1)$ where $0 < x < 1/5$
 (a) 1
 (b) 0
 (c) -1
 (d) $1/5$
 Ans (b)
- 9 The function $f(x) = |x - 2| + 3, x \in \mathbb{R}$ is 2
 (a) discontinuous at $x = 3$.
 (b) discontinuous at $x = 2$.
 (c) continuous everywhere in \mathbb{R} .
 (d) discontinuous everywhere in \mathbb{R}
 Ans (c)
- 10 The function $f : \mathbb{R} \rightarrow \mathbb{R}, f(x) = 2x^2 - 8$ 1
 (a) is continuous at x in \mathbb{R}
 (b) Discontinuous at $x=2$
 (c) Discontinuous at $x=8$
 (d) Discontinuous in \mathbb{R}
 Ans (a)
- 11 Let $f(x) = \begin{cases} 2x + 4 & \text{if } x < 4 \\ 3b & \text{if } x \geq 4 \end{cases}$. If f is continuous on \mathbb{R} then the value of Y is 3
 (a) 2
 (b) 4
 (c) 3
 (d) 6
 Ans (b) 4
- 12 If $f: \mathbb{R} \rightarrow \mathbb{R}$, and $f(x) = 9$ then $\lim_{x \rightarrow 4} x^4 f(x) =$ 1
 (a) 4
 (b) 9
 (c) 36
 (d) 13
 (b)
- 13 Consider $f, g : \mathbb{R} \rightarrow \mathbb{R}$ and $c \in \mathbb{R}$. Under which of the following condition 1

does $\lim_{x \rightarrow c} f(x)g(x) = 0$ is true

(a) $\lim_{x \rightarrow c} f(x) = 0$

(b) $\lim_{x \rightarrow c} f(x) = L$ and $L \neq 0$ and $g(x)$ is bounded

(c) $\lim_{x \rightarrow c} g(x) = L$ and $f(x)$ is bounded

(d) $\lim_{x \rightarrow c} f(x) = L$ and $\lim_{x \rightarrow c} g(x) = 1/L$, $L \neq 0$

Ans : (a)

14 $\lim_{x \rightarrow \pi/4} \tan x =$

(a) 1

(b) $1/2$

(c) 1/

(d) 0

Ans (a)

15 $\lim_{x \rightarrow 0} x^2 \sin() =$

(a) 0

(b) 1

(c) $\pi/2$

(d) does not exist

Ans (b)

s

16 $\lim_{x \rightarrow \pi/2} e^{\cos x} =$

(a) e

(b) 0

(c) 1

(d) Not defined

Ans ©

17 $\cos(\log(x^2 - 2x + 2 + \sin(2x - 2))) =$

(a) 0

(b) $\pi/2$

(c) 1

(d) Does not exist

Ans : (c)

18 $e^{(x + \sin x - \cos x)} =$

(a) 1

(b) e

(c) 1/e

(d) Does not exist

Ans: (c)

19

If $f(x) = L$ and M , =

(a) L/M

(b) M/L

1

1

1

1

1

1

- (c) L
(d) M
Ans : (a)
- 20 2
The function defined by $f(x) = \begin{cases} x^2 & \text{if } x > 0, \\ 1 & \text{if } x = 0 \\ x^3 & \text{if } x < 0 \end{cases}$ then f is continuous at 5, _____
- (a) Only at $x = 0$
(b) at every $x \in \mathbb{R}$
(c) on $\mathbb{R} \setminus \{0\}$
(d) no where
Ans : (d)
- 21 3
Amongst the following, the false statement is _____
(a) There exists a function $f : \mathbb{R} \rightarrow \mathbb{R}$, which is discontinuous only at one point.
(b) There exists a function $f : \mathbb{R} \rightarrow \mathbb{R}$, which is continuous only at one point.
(c) At least one of (a) and (b) is true.
(d) At least one of (a) and (b) is false.
Ans ©
- 22 4
3 is a removable discontinuity of
(a)
(b) $1/\sin(x - 3)$
(c) $(x + 3)/(x - 3)$
(d)
Ans (d)
- 23 1
If $|f(x)| = L$ then
(a) $f(x) = |a|$
(b) $f(x) = a$
(c) $f(x)$ does not exist
(d) $f(x)$ may or may not exist
Ans (d)
- 24 1
If $\lim_{x \rightarrow a} f(x) = L$, which one of the following expressions is necessarily true?
(a) f is continuous at $x = a$
(b) $f(a)$ does not exist.
(c) $f(a) = L$
(d) $\lim_{x \rightarrow a^+} f(x) = L$.
Ans (d)

25. The function $f : [a, b] \rightarrow \mathbb{R}$ is continuous on $[a, b]$ then 1
 (a) f is not bounded
 (b) f is bounded but does not attain its bounds
 (c) f is bounded and attains its bounds
 (d) f is differentiable

Ans (c)

26. The function defined by $f(x) = \begin{cases} x^2 & \text{if } x > 2 \\ x^3 & \text{if } x \leq 2 \end{cases}$ is continuous 1
 _____.
 a.) Everywhere (b) at 2 (c) on $\mathbb{R} \setminus 2$ (d) None of these

Answer 3

27. The function defined by $f(x) = e^{2x}$ is continuous _____. 1
 a.) Only when x is a rational number (b) only when x is an irrational number
 (c) at every real number (d) nowhere

Answer 3

28. The function defined by $f(x) = \begin{cases} 1, & x \in \mathbb{Q} \\ -1, & x \in \mathbb{R} \setminus \mathbb{Q} \end{cases}$ is continuous 1
 _____.
 a) at every rational number only (b) at every irrational number only
 (c) at every real number (d) nowhere

Answer 4

29. The function defined by $f(x) = \begin{cases} x, & x \in \mathbb{Q} \\ -x, & x \in \mathbb{R} \setminus \mathbb{Q} \end{cases}$ is continuous _____. 1
 a) at every rational number only (b) at every irrational number only
 (c) only at 0 (d) nowhere

Answer 3

30. The function defined by $f(x) = \begin{cases} x \sin(1/x) & \text{if } x \neq 0 \\ a & \text{if } x = 0 \end{cases}$ is continuous at 1
 0, _____.
 a) If $a=1$ (b) if $a=-1$ (c) if $a=0$ (d) None of these

Answer 1

31. The function $f(x) = \dots$, for x is 1
 a) continuous and bounded b) continuous and not bounded
 c) discontinuous d) none of these

Answer 1

32. Every bounded sequence in 1

a) has at least one convergent subsequence b) has only one convergent subsequence

c) is always convergent d) is not convergent

Answer1

33 The polynomial x^2+1 has 1

a) no zero in \mathbb{R} b) one zero in \mathbb{R} c) two zeros in \mathbb{R} d) none of these

Answer1

34 = 1

a) 0 b) 1 c) -1 d) does not exist

Answer1

35 The value of 1

a) $1/3$ b) 1 c) $5/7$ d) 0

Answer3

36 The value of 1

(a) 1

(b) $1/7$

(c) 0

(d) 7

Answer3

37 The value of 1

a) 4 b) 0 c) 1 d) -1

Answer1

38 The function defined by $f(x) = \begin{cases} x-2 & \text{if } x \neq 2 \\ a & \text{if } x = 2 \end{cases}$ is continuous at 2 if $a =$, 1

a) 0 b) 1 c) 2 d) -2

Answer1

39 The value of 1

a) 4 b) 12 c) 1 d) -1

Answer2

40 The function defined by $f(x) = \begin{cases} x^2 & \text{if } x > 2 \\ 4 & \text{if } x \leq 2 \end{cases}$ is continuous 1

_____.
a.) Everywhere (b) at 2 (c) on $\mathbb{R} \setminus 2$ (d) None of these

Answer2

41 The function defined by $f(x) = \begin{cases} \sin x & \text{if } x \geq s \\ \cos x & \text{if } x < s \end{cases}$ is continuous _____ 2

a.) Everywhere (b) only at (c) on $\mathbb{R} \setminus$ (d) nowhere

Answer1

- 42 The function defined by $f(x) = \begin{cases} x^2+1 & \text{if } x \neq 5 \\ a & \text{if } x=5 \end{cases}$ is continuous at 5. 2
a) For any $a \in \mathbb{R}$ (b) if $a=6$ (c) if $a=26$ (d) None of these

Answer3

- 43 The function defined by $f(x) = \begin{cases} \cos x + 1 & \text{if } x \neq \pi \\ a & \text{if } x = \pi \end{cases}$ is continuous at π _____ . 2
a) For any $a \in \mathbb{R}$ (b) if $a=1$ (c) if $a=0$ (d) None of these

Answer3

- 44 The function defined by $f(x) = \begin{cases} x^2 & \text{if } x > 0 \\ 1 & \text{if } x = 0 \\ x^3 & \text{if } x < 0 \end{cases}$ is continuous _____ . 2
a) Only at $x=0$ (b) $\forall x \in \mathbb{R}$ (c) $\forall x \in \mathbb{R} \setminus \{0\}$ (d) nowhere is continuous

- 45 Amongst the following, the false statement is _____ . 3
a. There exists a function $f: \mathbb{R} \rightarrow \mathbb{R}$, which is discontinuous only at one point.
b. There exists a function $f: \mathbb{R} \rightarrow \mathbb{R}$, which is continuous only at one point.
c. At least one of (a) and (b) is true.
d. At least one of (a) and (b) is false

Answer4

- 46 The function defined by $f(x) = \begin{cases} \sin x + 1 & \text{if } x \neq \pi \\ a & \text{if } x = \pi \end{cases}$ is continuous at π _____ . 2
a) For any $a \in \mathbb{R}$ (b) if $a=1$ (c) if $a=0$ (d) None of these

Answer2

- 47 The function defined by $f(x) = \begin{cases} x^3+1 & \text{if } x \neq 5 \\ a & \text{if } x=5 \end{cases}$ is continuous at 5. 2
a) For any $a \in \mathbb{R}$ (b) if $a=6$ (c) if $a=126$ (d) 26

Answer3

- 48 The function defined by $f(x) = \begin{cases} \sec x + 1 & \text{if } x \neq \pi \\ a & \text{if } x = \pi \end{cases}$ is continuous at π . 2
a) For any $a \in \mathbb{R}$ (b) if $a=1$ (c) if $a=0$ (d) None of these

Answer3

- 49 The function defined by $f(x) = \begin{cases} x^3 + 1 & \text{if } x \neq 4 \\ a & \text{if } x = 4 \end{cases}$ is continuous at 4. 2
a) For any $a \in \mathbb{R}$ (b) if $a=65$ (c) if $a=126$ (d) 25

- 50 The function defined by $f(x) = \begin{cases} x^4 + 1 & \text{if } x \neq 5 \\ a & \text{if } x = 5 \end{cases}$ is continuous at 5. 2
a) For any $a \in \mathbb{R}$ (b) if $a=26$ (c) if $a=126$ (d) 626

Answer4

Unit 2

- 51 Suppose $f(x)$ satisfies the following two conditions and $f(1) = 1$. Then the value of $f(7)$ is 3
a) 55 (b) 88 (c) 66 (d) 77

Answer3

52. Which of the following function is continuous at $x=0$ but not differentiable at $x=0$? 1
a) $f(x) = x^{-5/3}$ b) $f(x) = x^{-1/3}$ c) $f(x) = x^{1/3}$ d) $f(x) = x^{5/3}$

Answer4

53. Let $f(x) = \begin{cases} x^2 & \text{if } x < 0 \\ a & \text{if } x = 0 \\ x^2 & \text{if } x > 0 \end{cases}$ then $f(x)$ is 1
a) continuous and differentiable (b) continuous but not differentiable (c) differentiable but not continuous (d) not defined

Answer4

54. Let $f(x) = \begin{cases} x^2 & \text{if } x < 0 \\ a & \text{if } x = 0 \\ x^2 & \text{if } x > 0 \end{cases}$ at the function is 1
a) Continuous but not differentiable (b) Differentiable but not continuous (c) Differentiable (d) Not continuous and not differentiable

Answer4

55. Let $f(x)$ be a differentiable function where the line tangent to the graph of $f(x)$ at $x=1$ is $y = 2x - 1$. 1

, then

- a) , b)
- b) d)

Answer2

56. Let then the number of points where is not differentiable are 1
- a) b) c) d)

Answer1

57. Consider the following statements 1
- i) If is continuous at then is differentiable at
 - ii) If exists then is differentiable at
 - iii) If exists then is differentiable at
 - iv) If is differentiable at then
- a) Only (ii) is true c) (ii) and (iii) are true
 - b) (i) and (iii) are not true d) (i), (ii) and (iv) are true

Answer4

- 58 Let be differentiable functions with the following properties 3
- ii) . If and then
- a) b) c) d)

Answer1

57. Let be differentiable functions. If where 1
- then is
- a) b) c) d)

Answer2

- 58 If and then 1
- a) b) c) d)

Answer1

59 If then is 1
a) b) c) d)

Answer1

60 If then is 1
a) b) c) d)

Answer3

61 If then is (assuming is a function of) 1
a) b) c) d)

Answer2

62 If then is (assuming is a function of) is 1
a) b) c) d)

Answer3

63 If is the inverse function of and if then 1
a) b) c) d)

Answer4

64 Suppose and h is the inverse function of then 1
a) b) c) d)

Answer2

65 Let be differentiable functions. If and are inverses of each other and then 1
is
a) c)
b) d) cannot compute as data is
insufficient

Answer3

66 If then third order derivative 2

- a) $\cos x$ c)
c) d)

Answer3

67 Let , the function is 2

- a) Continuous but not differentiable at $x=0$ c) Differentiable at $x=0$
b) Differentiable but not continuous at $x=0$ except $x=0$ d) Differentiable everywhere

Answer1

68 2

Then

- a) Discontinuous at $x=0$ and not differentiable at $x=0$ c)
Differentiable at $x=0$
b) Differentiable but not continuous at $x=0$ d) continuous and not
Differentiable at $x=0$

Answer1

69 2

- a) Continuous but not differentiable at $x=0$ c) Differentiable at $x=0$
b) Differentiable but not continuous at $x=0$ d) Differentiable everywhere

Answer3

70 If $f(x) = \sin x$, $f^n(x) =$ 2

- a) $\sin(n\pi/2+x)$ b) $\sin(n\pi/2-x)$ c) $\cos(n\pi/2+x)$ d) $\cos(n\pi/2-x)$

Answer1

71 If $f(x) = \cos x$, $f^n(x) =$ 2

- a) $\sin(n\pi/2+x)$ b) $\sin(n\pi/2-x)$ c) $\cos(n\pi/2+x)$ d) $\cos(n\pi/2-x)$

Answer3

- 72 Let $f(x)$ be the function $f(x) = \begin{cases} x^2 & \text{if } x \leq 2 \\ 4 & \text{if } x > 2 \end{cases}$ is 2
- a) Continuous but not differentiable at $x=2$ c) Differentiable
 at $x=2$
 b) Differentiable but not continuous at $x=2$ d) Not continuous
 and not differentiable at $x=2$

Answer3

- 73 If $y = a^x$ then $y_2 =$ 2
- a) a^x b) $a^x \log a$ c) $a^x (\log a)^2$ d) 0

Answer3

- 74 If $y = x^m$ then $y_2 =$ 2
- a) m b) m^2 c) $m!$ d) m^m

Answer3

- 75 If $y = \cos x$ then third order derivative is 2
- a) $\cos x$ c) $-\cos x$
 b) $-\sin x$ d) $\sin x$

Answer3

- 76 The given function is differentiable at c if the graph of the function has 1
- (a) a unique non vertical tangent at c
 (b) has many tangent nonvertical tangent at c
 (c) a unique vertical tangent at c
 (d) has more than vertical tangent at c

Ans : (a)

- 77 Which of the following functions is continuous at $x = 0$ but not differentiable at $x = 0$? 2
- (a) $x^{-4/3}$.
 (b) $x^{-1/3}$.
 (c) $x^{1/3}$.
 (d) $x^{4/3}$.

Ans : (d)

- 78 Let $f(x) = \begin{cases} x^2 & \text{if } x \leq 2, \\ 8 - 2x & \text{if } x > 2. \end{cases}$ 3
- Then f is

- (a) continuous but not differentiable at $x = 2$.
- (b) Not continuous at $x = 2$ but differentiable at $x = 2$.
- (c) Differentiable at $x = 2$.
- (d) Neither continuous nor differentiable at $x = 2$.

Ans : (a)

- 79 Let $f(x) = |x - 2| + |x - 3|$, for all $x \in \mathbb{R}$ then $f'(2) = ?$ 1
- (a) -2
 - (b) 0
 - (c) 3
 - (d) not defined.

(d)

- 80 f is differential at $x = a$ there for f is 1
- (a) continuous at $x = a$
 - (b) not continuous at $x = a$
 - (c) $1/f$ is differential at $x = a$
 - (d) $1/f$ is never differential at $x = a$

Ans : (a)

- 81 $f: \mathbb{R} \rightarrow \mathbb{R}$ is differentiable at $x = a$, if f is even, then 1
- (a) f' is odd
 - (b) f' is even
 - (c) f' is constant
 - (d) $f' = 0$

Ans (a)

- 82 f^2 is differentiable in on \mathbb{R} therefor 1
- (a) f is differentiable
 - (b) f is differentiable at some point of \mathbb{R}
 - (c) f is continuous at least some point of \mathbb{R}
 - (d) May or may not continuous and differentiable

Ans (d)

- 83 $f(x) = |x-7|$, x in \mathbb{R} is 1
- (a) Differentiable at $x=7$
 - (b) Differentiable in \mathbb{R}
 - (c) Not differentiable on $x = 7$
 - (d) Not differentiable on $\mathbb{R} - \{0\}$

Ans : (c)

- 84 The function $\tan x$ is 2
- (a) Well- defined on \mathbb{R}
 - (b) Differentiable on \mathbb{R}
 - (c) Not differentiable anywhere on \mathbb{R}
 - (d) Differentiable on $n\pi$

Ans : (d)

- 85 The function $e^{2\cos x}$ is 3
- (a) Differentiable on \mathbb{R}

(b) Not differentiable anywhere on \mathbb{R}

(c) Not differentiable at $x = 0$

(d) Not differentiable at $x =$

Ans (a)

86 The derivative of the inverse function of $f(x) = 8x + x^2$, x in \mathbb{R} at $x=20$ is 2

(a) $1/12$

(b) 12

(c) $1/48$

(d) 48

Ans : (d)

87 The derivative of the inverse function of $f(x) = x^3 - 4x + 1$ in \mathbb{R} at $x=2$ 2

(a) 4

(b) $1/4$

(c) $1/8$

(d) 8

Ans: ©

88 If $y = \sin(ax+b)$, where a, b in \mathbb{R} , then $y_n =$ 1

(a) $a^n \sin(ax+b +)$

(b) $a^n \cos(ax+b +)$

(c) $a^n \sin(ax+b +)$

(d) $a^n \cos(ax+b +)$

Ans : (a)

89 $y = \sin(a+b)$, where a, b in \mathbb{R} , then $y_n =$ 1

(a) $a^n \sin(ax+b +)$

(b) $a^n \cos(ax+b +)$

(c) $a^n \sin(ax+b +)$

(d) 0

Ans (d)

90 The n th derivative of xe^x is 4

(a) e^x

(b) $x^n e^x$

(c) $x e^{nx}$

(d) $x e^x + n e^x$

Ans : (d)

91 $Y = \cos(2x+5)$ then $y_{10} =$ 2

(a) $\sin(2x+5)$

(b) $2^{10} \cos(2x+5)$

(c) $2^{10} \cos(2x+5 +)$

(d) $2^{10} \cos(2x+5)$

Ans: (c) answer3

92 If $x = \cos \theta$, $y = \sin \theta$ then $dy/dx =$ 3

(a) $\tan^3 \theta$

(b) $\tan \theta$

(c) $-\tan \theta$

(d) $\cot \theta$

Ans : (c)

93 If $x^2 + 2xy = y^2$ then dy/dx is (assuming y is a function of x) 2

(a) .

(b) .

(c) $2x + 2y$.

(d) $(x + 1)/y$.

Ans : (b)

94 If h is the inverse function of f and if $f(x) = 1/x$ then $h'(3) =$ 2

(a) 9

(b) $1/9$

(c) -9

(d) $-1/9$

Ans : (c)

95 Let $f, g : \mathbb{R} \rightarrow \mathbb{R}$ be differentiable functions. If f and g are inverses of each other and $f'(2) = 5$ and $g'(2) = ?$ 1

(a) -5.

(b) $1/5$.

(c) $-1/5$.

(d) Cannot calculate as data is insufficient.

Ans (b)

96 $f : \mathbb{R} \rightarrow \mathbb{R}$ is a differentiable function where the tangent to the graph of $f(x)$ at $x = 2$ is $y = x + 1$, then

(a) $f(2) = 1, f'(2) = 1$.

(b) $f(2) = 1, f'(2) = 0$.

(c) $f(2) = 3, f'(2) = 1$.

(d) $f(2) = 3, f'(2) = 0$.

Ans (c)

97 If $y =$ then $y_s =$ 1

(a)

(b)

(c)

(d)

Ans (a)

Unit 3

98 Point of inflection of $f(x) = x^3 + 2x^2 - 4$ 2

(a) $-2/3$

(b) $2/3$

(c) $3/2$

(d) $-3/2$

Ans (a)

99 $F(x) = e^x$ is always 1

- (a) Concave upward everywhere
- (b) Concave downward everywhere
- (c) Concave upward only $x > 0$
- (d) Concave downward for $x > 0$

Ans (a)

100 Which of the following functions is increasing on the interval $(-\pi/2, \pi/2)$? 1

- (a) x^2
- (b) $\cos x$
- (c) $\sin x$
- (d) $|x|$

Ans : (c)

101 The function $y = x^2$ is increasing on 1

- (a) \mathbb{R}
- (b) $(-, 0)$
- (c) $(0, \infty)$
- (d) Its decreasing function every where

Ans (b)

102 The function $y = x^3 - 6x^2 + 9x - 3$ is increasing on 2

- (a) $(1, 3)$
- (b) \mathbb{R}
- (c) $(0, \infty)$
- (d) $(-\infty, 0)$

Ans : (a)

103 $F(x) = x^3 - 3x^2 + 3x + 2$ is 1

- (a) Monotonically decreasing
- (b) Monotonically increasing
- (c) Monotonically non decreasing
- (d) Monotonically non increasing

Ans : (b)

104 Let $f : [a, b] \rightarrow \mathbb{R}$ be a function such that f is continuous on $[a, b]$, differentiable on (a, b) and $f(a) = f(b)$. Then 1

- (a) there exists a unique $c \in (a, b)$ such that $f'(c) = 0$.
- (b) there exists $c \in (a, b)$ such that $f(c) = 0$.
- (c) there exists $c \in (a, b)$ such that $f''(c) = 0$.
- (d) there exists $c \in (a, b)$ such that $f''(c) = 0$.

Ans : (c)

105 Let $f : [a, b] \rightarrow \mathbb{R}$ be a function such that f is continuous on $[a, b]$ and differentiable on (a, b) . Then 1

- (a) there exists a unique $c \in (a, b)$ such that $f'(c) = 0$.
- (b) there exists $c \in (a, b)$ such that $f'(c) = 0$.

- (c) there exists $c \in (a, b)$ such that $f(c) = .$
 (d) there exists $c \in (a, b)$ such that $f''(c) = .$

Ans :

- 106 For a given function, $y = f(x)$, it is found that $f'(c) = 0$. Therefore, 1
 (a) c must be a point of local maximum of f
 (b) c must be a point of either local maximum or local minimum of f
 (c) c must be a point of local minimum of f .
 (d) nothing can be said about c .

Ans : (b)

- 107 The function $y = e^x$ is concave upwards 1
 (a) only at the origin
 (b) over negative real numbers only.
 (c) over positive real numbers only
 (d) Everywhere

Ans (d)

- 108 The function $y = \ln x$ is concave downwards 1
 (a) only at 1
 (b) over positive rational numbers only.
 (c) over positive irrational numbers only.
 (d) wherever it is defined.

Ans (d)

- 109 The n^{th} Taylor polynomial of $\sin x$ around 0 is given by 1
 (a) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$.
 (b) $1 + x - \frac{x^2}{2!} + \frac{x^3}{3!} - \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$.
 (c) $x + \frac{x^3}{3!} - \frac{x^5}{5!} + \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$.
 (d) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$.

Ans : (a)

- 110 The n^{th} Taylor polynomial of e^x around 0 is given by 1
 (a) $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$.
 (b) $1 + x - \frac{x^2}{2!} + \frac{x^3}{3!} - \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$
 (c) $x + \frac{x^3}{3!} - \frac{x^5}{5!} + \dots + \frac{x^n}{n!}$ where $n = 2k$ or $n = 2k - 1$.
 (d) $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!}$

Ans: (d)

- 111 $F(x) = xe^x$, x in R is 1
 (a) Increasing if $x > -1$
 (b) Decreasing if $x > 0$
 (c) Neither increasing nor decreasing
 (d) Increasing everywhere

Ans : (a)

- 112 $F(x) = x - x^2$ in x in R is 2
 (a) F is concave upward everywhere
 (b) F is concave downward everywhere
 (c) Concave upward only if $x > 0$

- (d) Concave downward if $x > 0$
 Ans : (b)
- 113 $F(x) = x^6 + x^2$, x in \mathbb{R} is 2
 (a) F is concave upward everywhere
 (b) F is concave downward everywhere
 (c) F Concave upward only if $x > 0$
 (d) F Concave downward if $x > 0$
 Ans : (a)
- 114 The value of 1
 (a) 1
 (b) -1
 (c) $9/2$
 (d) 0
 Ans: (c)
- 115 The value of $\log_c 10$ is 1
 (a) 1
 (b) $\log_c 10$
 (c) $\log_{10} 10$
 (d) 0
 Ans: (b)
- 116 $F(x) = x^3 - 12x + 1$ has local minima at 2
 (a) $X = 2$
 (b) $X = -2$
 (c) $X = 0$
 (d) $X = -1$
 Ans (b)
- 117 The value of $c \in (0, 2)$ for $f(x) = \cos x$ by Rolle's theorem 2
 (a) 1
 (b) -1
 (c)
 (d)
 Ans : (c)
- 118 $f(x) = 10 - 12x - 3x^2 - x^3$ in x in \mathbb{R} is 3
 (a) Increasing everywhere
 (b) Decreasing everywhere
 (c) Decreasing at $x = -2$
 (d) Increasing at $x = 2$
 Ans : (b)
- 119 $f(x) = x - 2 \sin x$, $0 < x < 3\pi$, has minimum value at 2
 (a) $\pi/3$
 (b) $2\pi/6$
 (c) $\pi/6$
 (d) 0

Ans : (c)

- 120 $f(x) = x^2 - 5x + 9$, $x \in [1, 4]$ what is value of c , by Rolle's theorem 1
- (a) $2/5$
 - (b) $5/2$
 - (c) $-2/5$
 - (d) $-5/2$

Ans : (b)

- 121 If f is continuous at the point and curve changes from concave upward to concave downward or vice versa is called 1
- (a) Point of inflection
 - (b) Maximum at a point
 - (c) Minimum at a point
 - (d) increasing

Ans : (a)

- 122 $F(x) = 5x^2 - 2x$ has critical point at 1
- (a) 5
 - (b) $1/5$
 - (c) -5
 - (d) $-1/5$

Ans : (d)

- 123 $F(x) = x^2 - 8x + 5$ has critical point at 2
- (e) 4
 - (f) -4
 - (g) 2
 - (h) 8

Ans 1

- 124 The function $y = f(x)$ is decreasing at c , if 2
- (a) , whenever and , whenever .
 - (b) , whenever and , whenever .
 - (c) , whenever and , whenever .
 - (d) all of these

Answer1

- 125 Tangent of the curve of $F(x) = x^2 + 2x + 1$ is parallel to line $y = 4x + 3$ 2
- (a) 2
 - (b) 1
 - (c) 4
 - (d) 6

Answer2

- 126 The function is increasing at c , if 1
- (a) , whenever and , whenever .

(b) , whenever and , whenever .

(c) , whenever and , whenever .

(d) none of these

Answer2

127 Let a and b be such that . Then, there exists c between a and b such that 1

(a) (b)

(c) (d) none of these

Answer1

128 Let a function f be continuous on $[a, b]$ and differentiable on (a, b) . Then 1

(a) there exists a unique such that

(b) there exists such that

(c) there exists such that

(d) none of these

Answer3

129 = 1

(a) 0 (b) 1 (c) (d) None of these

Answer1

130 Let a function f be continuous on $[a, b]$, differentiable on (a, b) and let $f(a) = f(b)$. Then 1

(a) there exists a unique such that .

(b) there exists such that .

(c) there exists such that .

(d) none of these

Answer3

131 = 1

(a) 1 (b) 0 (c) a (d) None of these

Answer1

- 132 The function is decreasing at c , if 1
- (a) , whenever and , whenever .
 (b) , whenever and , whenever .
 (c) , whenever and , whenever .
 (d) none of these

Answer3

- 133 Which of the following functions is increasing at the origin? 1
- (a) (b) (c) (d)

Answer4

- 134 = 1
- (a) 2 (b) 1 (c) 0 (d) None of these

- 135 = 1
- (a) 1 (b) 0 (c) (d) None of these

Answer1

- 136 = 1
- (a) 0 (b) 1 (c) (d) None of these

Answer2

- 137 The function is decreasing on 1
- (a) (b) (c) (d) None of these

- 138 The function is increasing on 1
- (a) (b) (c) (d) None of these

Answer1

- 139 The function is decreasing on 1
- (a) (1, 3) (b) (c) (d) None of these

Answer1

- 140 The function is increasing on 1
- (a) (b) (c) (d) None of these

Answer3

- 141 Which of the following functions is decreasing at the origin? 1
(a) (b) (c) (d)

Answer1

- 142 The function attains its maximum value at 1
(a) 1 (b) -1 (c) 0 (d) None of these

- 142 The function attains its minimum value 1
(a) at exactly one point (b) at only finitely many points
(c) at infinitely many points (d) nowhere

Answer3

- 143 For a given function, f , it is found that $f'(c) = 0$. Therefore, 1
(a) c must be a point of local maximum of f .
(b) c must be a point of local minimum of f .
(c) c must be a point of either local maximum or local minimum of f .
(d) nothing can be said about c .

Answer3

- 144 The function is concave downwards 1
(a) only at 1 (b) over positive rational numbers only
(c) over positive irrational numbers only (d) wherever it is defined

Answer2

- 145 The function is concave upwards 1
(a) only at the origin (b) over negative real numbers only
(c) over positive real numbers only (d) everywhere

Answer4

- 146 A triangle with the given perimeter has maximum area if and only if it is 2

(a) obtuse angled (b) isosceles (c) right angled (d) equilateral

Answer4

147 A rectangle with the given perimeter has maximum area if and only if it is a 2

(a) rhombus (b) parallelogram (c) square (d) kite

Answer3

148 The function , has local maximum at 2

(a) (b) (c) 0 (d) None of these

Answer1

149 Amongst the following, the function, which has a local minimum at the 2
origin, is

(a) (b)
(c) (d)

Answer4

150 Amongst the following, the function, which has a local maximum at the 2
origin, is

(a) (b)
(c) (d)

Answer1